Engaging Students in Math Practices

When the most recent mathematical content standards were written, authors recognized the need for changes to instruction in addition to new content standards. Called Practice Standards in the Common Core State Standards (CCSS) and Process Standards in other states, these instructional practices were based on research from National Council of Teachers of Mathematics (NCTM) and the National Research Council's report *Adding It Up*. The NCTM process standards included problem solving, reasoning and proof, communication, representation, and connections. Similarly, *Adding It Up* detailed five strands of mathematical proficiency: adaptive reasoning, strategic competence, conceptual understanding, procedural fluency, and productive disposition. The NCTM process standards and *Adding it Up* strands of mathematical proficiency led to the Standards for Mathematical Practice, which provide guidance for learners at all grade levels. The overarching goal of this course is to familiarize teachers with the Standards for Mathematical Practice in a way that is applicable across all states and to help develop students who are mathematically proficient.

This course provides an in-depth look at the eight mathematics practice standards that are applicable in all classrooms regardless of the content standards in your state. It allows teachers to explore ways to implement each standard in the classroom to ensure that students are given the opportunity to develop these practices in their own lives.

Course Objectives

By the end of this course, you will be able to

Module 1

- Distinguish between the eight mathematical practice standards.
- Compare and contrast the role of the mathematical practice standards and the role of the mathematical content standards.
- Extrapolate changes in instruction required to implement the mathematical practice standards.

Module 2

- Explain the major components of Mathematical Practice Standard 2 (MP2): reason abstractly and quantitatively; and Mathematical Practice Standard 3 (MP3): construct viable arguments and critique the reasoning of others.
- Evaluate a specific mathematical learning context and provide evidence of how MP2 and MP3 are applied or not applied in the situation.
- Hypothesize and reflect on why proficiency in mathematics requires students to be able to reason abstractly and quantitatively and to be able to construct viable arguments and critique the reasoning of others.

Module 3

- Extrapolate the meaning of Mathematical Practice 4 (MP4): model with mathematics; and Mathematical Practice 5 (MP5): use appropriate tools strategically.
- Design lesson plans that use appropriate tools strategically.
- Generate specific examples of mathematical modeling at the appropriate grade level.

Module 4

- Explain the components Mathematical Practice 7 (MP7): look for and express regularity in repeated reasoning; and Mathematical Practice 8 (MP8): look for and make use of structure in mathematics.
- Generate specific examples of and strategies for generalizing and seeing structure in mathematics.
- Generate specific examples of and strategies for looking for and making use of structure in mathematics.

Module 5

- Explain the components of MP1: make sense of problems and persevere in solving them; and Mathematical Practice 6 (MP6): attend to precision.
- Generate specific examples and strategies for ensuring students make sense of problems and persevere in solving them.

• Generate specific examples of and strategies for ensuring students attend to precision in mathematics.

Module 6

• Generate specific examples where more than two practice standards intersect in preparing proficient mathematics learners.

Implement strategies from this course in your own classroom.

Course Syllabus

Module 1	Introduction to the Mathematics Practice Standards
	Module Welcome
	Video 1: The Common Core Mathematics Classroom
	• Reading 1: What Are the Standards for Mathematical Practice?
	 Reading 2: ASCD Express—Content and Practice Standards Define New Roles in Math Classrooms
	Video 2: The Importance of Mathematical Practices
	Knowledge Check
	Application: Mathematics Practice Standards Lesson Plan
	Post-Module Reflection
Module 2	Reasoning and Explaining
Module 2	Reasoning and ExplainingModule Welcome
Module 2	 Reasoning and Explaining Module Welcome Reading 1: Higher-Order Thinking Is for Everyone
Module 2	 Reasoning and Explaining Module Welcome Reading 1: Higher-Order Thinking Is for Everyone Video 1: Mathematical Practice #2
Module 2	 Reasoning and Explaining Module Welcome Reading 1: Higher-Order Thinking Is for Everyone Video 1: Mathematical Practice #2 Video 2: Mathematical Practice #3
Module 2	 Reasoning and Explaining Module Welcome Reading 1: Higher-Order Thinking Is for Everyone Video 1: Mathematical Practice #2 Video 2: Mathematical Practice #3 Reading 2: <i>EL</i>—Go Figure: Math and the Common Core
Module 2	 Reasoning and Explaining Module Welcome Reading 1: Higher-Order Thinking Is for Everyone Video 1: Mathematical Practice #2 Video 2: Mathematical Practice #3 Reading 2: <i>EL</i>—Go Figure: Math and the Common Core Knowledge Check
Module 2	 Reasoning and Explaining Module Welcome Reading 1: Higher-Order Thinking Is for Everyone Video 1: Mathematical Practice #2 Video 2: Mathematical Practice #3 Reading 2: <i>EL</i>—Go Figure: Math and the Common Core Knowledge Check Application: Critique Reasoning and Explaining

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Module 3	Using Tools and Modeling
	Module Welcome
	Reading 1: Use of Tools in the Context of Mathematical Modeling
	Video 1: Mathematical Practice #4
	Video 2: Mathematical Practice #5
	• Reading 2: A Dutch Primer: Calculators for Enrichment in the Early Years
	Knowledge Check
	Application: Using Tools and Modeling
	Post-Module Reflection
Module 4	Generalizing and Seeing Structure
	Module Welcome
	Reading 1: Patterns, Patterns, Patterns
	Video 1: Mathematical Practice #7
	Video 2: Mathematical Practice #8
	Reading 2: <i>EL</i> —From Arithmetic to Algebra
	Knowledge Check
	Application: Implementing Structure and Generalizations
	Post-Module Reflection
Module 5	Developing Habits of Mind
	Module Welcome
	Reading 1: Problem Solving: The Essence of it All
	Video 1: Mathematical Practice #1
	Video 2: Mathematical Practice #6
	Reading 2: <i>EL</i> —Problem-Solving Time
	Knowledge Check
	Application: Promoting Problem Solving
	Post-Module Reflection

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Module 6	Making the Practice Standards Intentional
	Module Welcome
	Video: Mathematical Practices, Focus, and Coherence in the Classroom
	Reading 1: Implementing Math Practices into Instruction
	Reading 2: EL—Instigating Thinking in Math Class
	Knowledge Check
	Application: Implementing Multiple Mathematics Practice Standards
	Post-Module Reflection

Resources

Module 1

Smith, N. (2012). Content and Practice Standards Define New Roles in Math Classrooms. *ASCD Express*, 7(21).

The Hunt Institute. (2011, August 19). The Importance of Mathematical Practices. Retrieved December 19, 2013, from YouTube: <u>https://www.youtube.com/watch?v=m1rxkW8ucAl&feature</u> <u>=youtu.be</u>

Thompson, J. (2012, June 28). *The Common Core Mathematics Classroom*. Retrieved December 19, 2013, from YouTube: <u>http://www.youtube.com/watch?v=7E-EGbB3N_0</u>

Module 2

- Big Ideas Learning (2011, November). *Mathematical Practice #2*. Retrieved December 19, 2013, from YouTube: <u>http://www.youtube.com/watch?v=sp8r5hIGFsQ</u>
- Big Ideas Learning (2011, November). *Mathematical Practice #3*. Retrieved December 19, 2013, from YouTube: <u>http://www.youtube.com/watch?v=4Brp578YJrw</u>
- Burns, M. (December 2012/January 2013). Go figure: Math and the common core. *Educational Leadership*, *70*(4), 42–46. Retrieved from <u>http://www.ascd.org/publications/educational-leadership/dec12/vol70/num04/Go-Figure@-Math-and-the-Common-Core.aspx</u>

Module 3

Big Ideas Learning (2011, November). *Mathematical Practice #4.* Retrieved December 19, 2013, from YouTube: http://www.youtube.com/watch?v=InTG8Bdq-ac

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- van den Brink, J. (2004). A Dutch primer: Calculators for enrichment in the early years. *Curriculum*•*Technology Quarterly, 13*(3). Retrieved from <u>http://www.ascd.org/publications/ctq/</u> <u>spring2004/A-Dutch-Primer@.aspx</u>

Module 4

- Big Ideas Learning (2011, November). *Mathematical Practice #7*. Retrieved December 19, 2013, from YouTube: http://www.youtube.com/watch?v=iZTu_hSjF0g
- Big Ideas Learning (2011, November). *Mathematical Practice #8*. Retrieved December 19, 2013, from YouTube: <u>http://www.youtube.com/watch?v=nDdYEBPZJSI</u>
- Ketterlin-Geller, L. R., Jungjohann, K., Chard, D.J., & Baker, S. (2007). From arithmetic to algebra. Educational Leadership, 65(3), 66–71.

Module 5

- Big Ideas Learning (2011, November). *Mathematical Practice #1*. Retrieved December 19, 2013, from YouTube: <u>http://www.youtube.com/watch?v=A59NM4gK5rs&list=PLkCODEjk2FRH25f</u> <u>Ohg Wfsk-cKSB5OZVQ&index=1</u>
- Big Ideas Learning (2011, November). *Mathematical Practice #6*. Retrieved December 19, 2013, from YouTube: http://www.youtube.com/watch?v=LITEv64v7vw
- Gurule, K. (2007). Problem-solving time. *Educational Leadership*, 65(3). Retrieved from http://www.ascd.org/publications/educational_leadership/nov07/vol65/num03/Problem-Solving_Time.aspx

Module 6

- Hiltabidel, J. (December 2012/January 2013). Instigating thinking in math class. *Educational Leadership*, *70*(4). Retrieved from <u>http://www.ascd.org/publications/educational-leadership/dec12/</u> <u>vol70/num04/Instigating-Thinking-in-Math-Class.aspx</u>
- NCTM (2013, January). *Mathematical Practices, Focus and Coherence in the Classroom*. Retrieved December 19, 2013, from YouTube: <u>http://www.youtube.com/watch?v=X1GwdACHdtY</u>